Graph Prompting for Graph Learning Models: Recent Advances and Future Directions

Presenters: Xingbo Fu, Zehong Wang, Jundong Li

University of Virginia, University of Notre Dame, University of Connecticut



KDD 2025 Tutorial
August 2025

Presenters



Xingbo Fu is a PhD candidate at the University of Virginia. His research interests focus mainly on graph learning, federated learning, and healthcare informatics. He has publications in major conferences and journals, such as KDD, ICLR, AAAI, ECAI, ICHI, SGIKDD Explorations, and TMLR. He brings industry experience through internships at Amazon and Netflix.



Zehong Wang is a PhD candidate at the University of Notre Dame. His research interests are broadly in machine learning and data mining, with a particular focus on foundation models. His work has appeared at top-tier conferences such as KDD, NeurIPS, ICML, IJCAI, NAACL, ACL, SDM, and WSDM. He has also applied his expertise in industry as an Applied Scientist Intern at Amazon.



Jundong Li is an Associate Professor at the University of Virginia. His research interests are generally in data mining and machine learning, with a focus on graph machine learning, trustworthy/safe machine learning, and LLMs. He has received several prestigious awards, including the SIGKDD Rising Star Award (2024), the SIGKDD Best Research Paper Award (2022), and the NSF CAREER Award (2022).



Tutorial Outline

Time	Section	
1:00pm ~ 1:30pm	Section 1: Introduction	
1:30pm ~ 2:00pm	Section 2: Graph Pre-training for Graph Prompting	
2:00pm ~ 3:00pm	Section 3: Techniques in Graph Prompting	
3:00pm ~ 3:30pm	Coffee Break	
3:30pm ~ 3:45pm	Section 4: Summary and Future Directions	
3:45pm ~ 4:00pm	Section 5: Q&A	



Tutorial Website & Survey Paper

Tutorial website

Slides & more information about this tutorial

https://www.xingbofu.com/tutorials/kdd25-graph-promptng



Graph Prompting for Graph Learning Models: Recent Advances and Future Directions

Xingbo Fu, Zehong Wang, Zihan Chen, Jiazheng Li, Yaochen Zhu, Zhenyu Lei, Cong Shen, Yanfang Ye,

Chuxu Zhang, Jundong Li

https://arxiv.org/abs/2506.08326



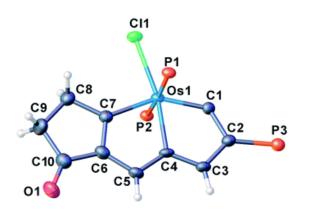


August 3-7, 2025 August 3-7, 2025 August 3-7, 2025

Section 1 Introduction

Jundong Li
Associate Professor
University of Virginia

Graphs



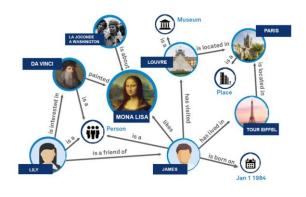
Molecular graphs



Social network



Transportation network



Knowledge graph

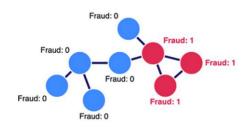


Modeling Real-World Data as Graphs

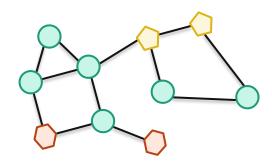
A graph $G = (\mathcal{V}, \mathcal{E}, \mathbf{X})$

- $\mathcal{V} = \{v_1, v_2, \dots, v_N\}$: the node set
- $\mathcal{E} \subseteq \mathcal{V} \times \mathcal{V}$: the edge set
- $X \in \mathbb{R}^{N \times F}$: node feature matrix
- $A \in \{0,1\}^{N \times N}$: adjacency matrix

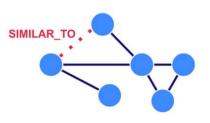
Tasks for graphs



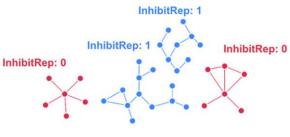
Node-level tasks



A graph $G = (\mathcal{V}, \mathcal{E}, \mathbf{X})$



Edge-level tasks



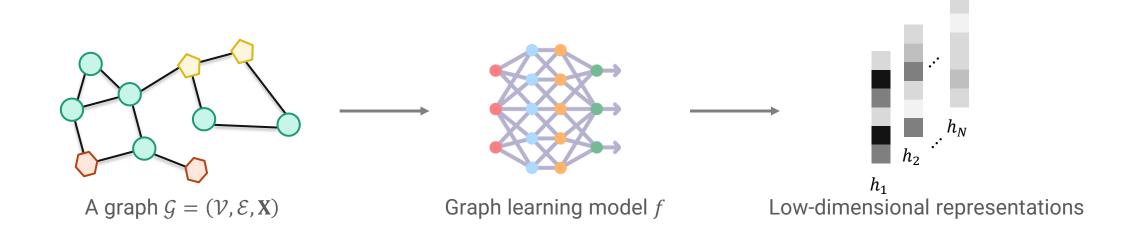
Graph-level tasks



Graph Representation Learning

Learn expressive graph representations by training graph learning models

Graph embeddings can be used for downstream tasks

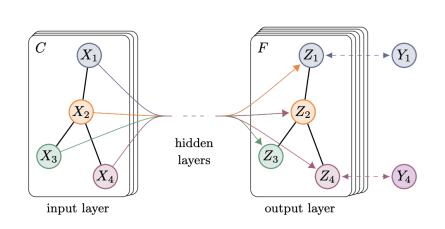


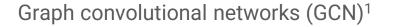


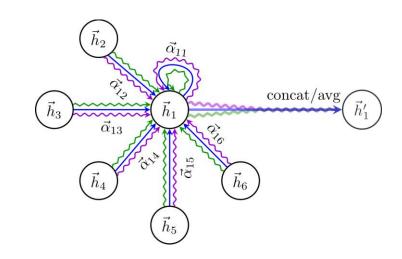
Graph Learning Models

Graph neural networks (GNN)

Iteratively aggregate information in the neighborhood via the message-passing mechanism





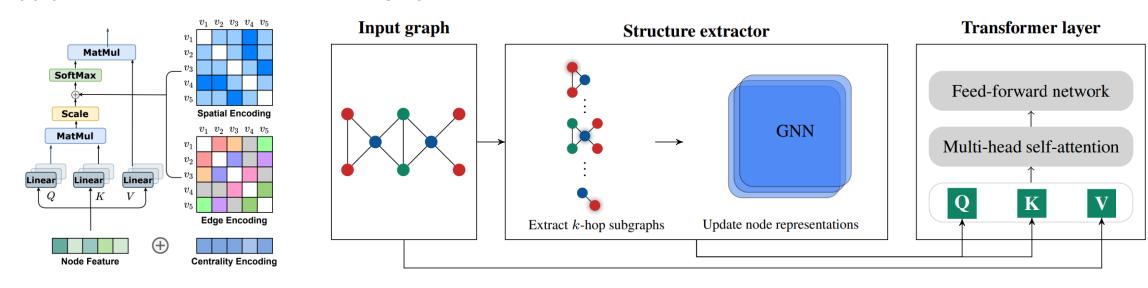


Graph attention networks (GAT)²

Graph Learning Models

Graph Transformers (GT)

Apply Transformer architectures to graph data



Graphormer¹

Structure-aware Transformer (SAT)²



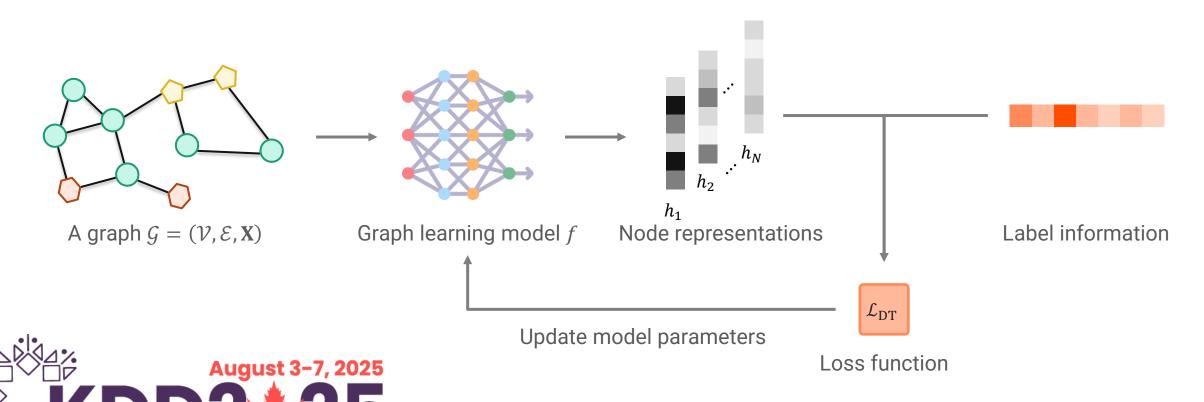
[1] Ying, Chengxuan, et al. "Do Transformers Really Perform Badly for Graph Representation?." NeurIPS 2021.

[2] Chen, Dexiong, et al. "Structure-Aware Transformer for Graph Representation Learning." ICML 2022.

Traditional Training Paradigm for Graph Learning Models

End-to-end training

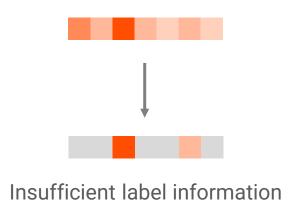
Optimize graph learning models based on abundant label information



Limitations of Traditional Training Paradigm

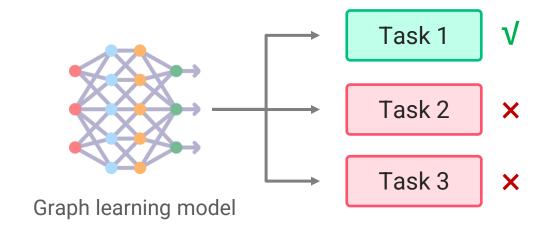
Rely heavily on label information

 Sufficient labeled graph data may be inaccessible in practice



Poor generalization

 Graph learning models cannot be well generalized to other downstream tasks

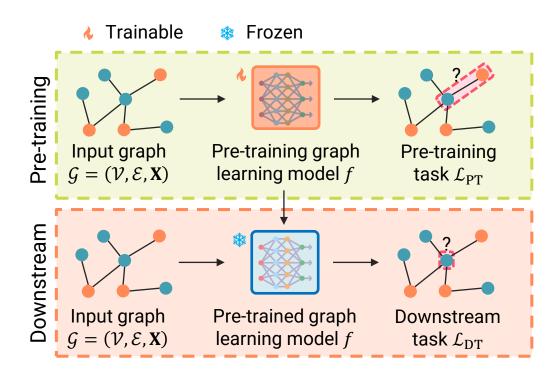




Graph Pre-training via Self-supervised Learning

Learn generalizable graph embeddings without label information

- Pre-training stage
- Graph learning models are learned by solving hand-crafted auxiliary tasks \mathcal{L}_{PT}
- Supervision signals are acquired from graph data itself
- Downstream tasks
- Pre-trained graph learning models directly generate graph embeddings used for downstream tasks \mathcal{L}_{DT}





Objective Gap between Pre-training and Downstream Tasks

Example: edge prediction → **node classification**

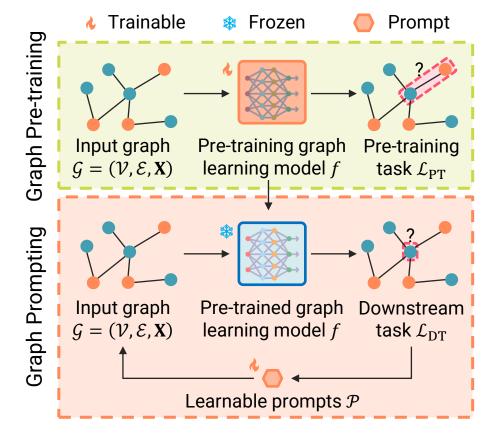
Phase	Pre-training stage	Downstream stage
Illustration		?
Task	Edge prediction	Node classification
Involved embeddings	A pair of nodes	A single node
Prediction	Edge probabilities	Node class probabilities



The "Pre-training, Prompting" Scheme

Two-stage adaptation of pre-trained graph learning models

- Stage 1: graph pre-training via self-supervised learning
- A graph learning model f is pre-trained on a pre-training task $\mathcal{L}_{\mathrm{PT}}$
- Stage 2: graph prompting for adaptation
- Adapt the pre-trained graph learning model f for the downstream task $\mathcal{L}_{\mathrm{DT}}$ by learning extra prompts \mathcal{P}
- The pre-trained graph learning model *f* keeps frozen



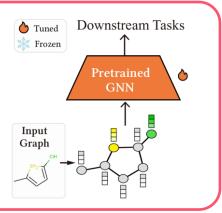
The "pre-training, prompting" scheme for graph learning models



Comparison between Graph Fine-tuning & Graph Prompting

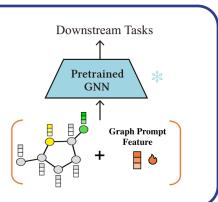
Graph fine-tuning

- Adapt pre-trained graph learning models by further tuning model parameters
- Tunable parameters: the whole graph learning model
- Unchanged part: graph data



Graph prompting

- Adapt pre-trained graph learning models by learning extra prompts
- Tunable parameters: additional prompts
- Unchanged part: the pre-trained graph learning model

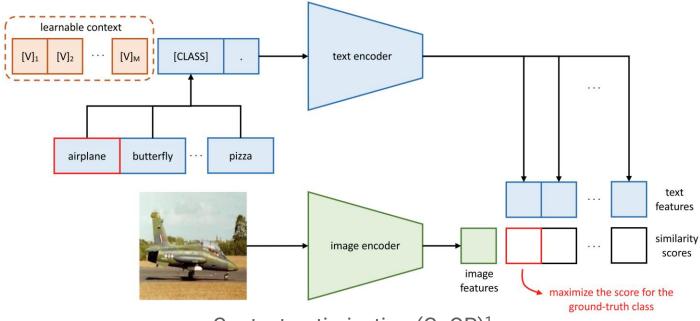




Prompting in NLP and CV

Learning to modify the input data with extra trainable prompts

Prompting in NLP: learn extra trainable tokens



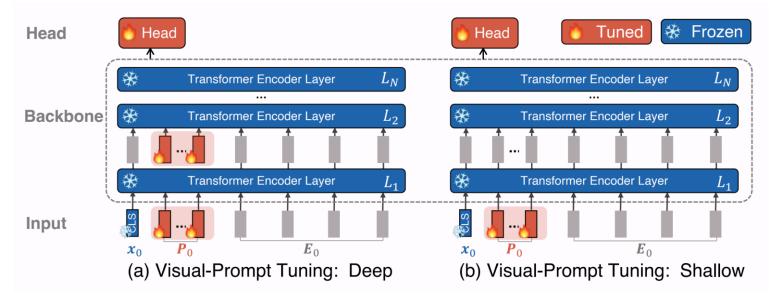
Context optimization (CoOP)¹



Prompting in NLP and CV

Learning to modify the input data with extra trainable prompts

Prompting in CV: learn extra trainable patches



Visual prompt tuning (VPT)¹



Challenges in Prompting for Graph Learning Models

Non-Euclidean graph data

Important structural information in graph data

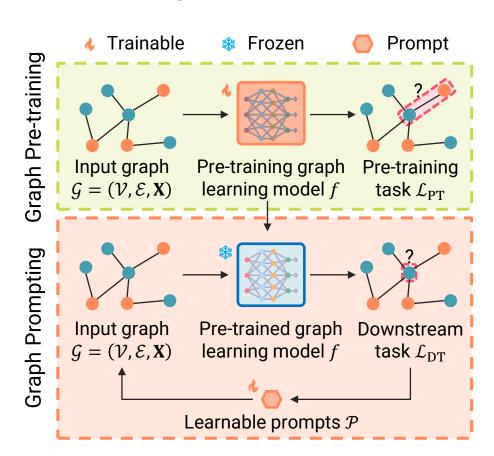
Pre-training compatibility

- Pre-training strategies: generative/contrastive/...
- Should be compatible with various pre-training strategies

Downstream task universality

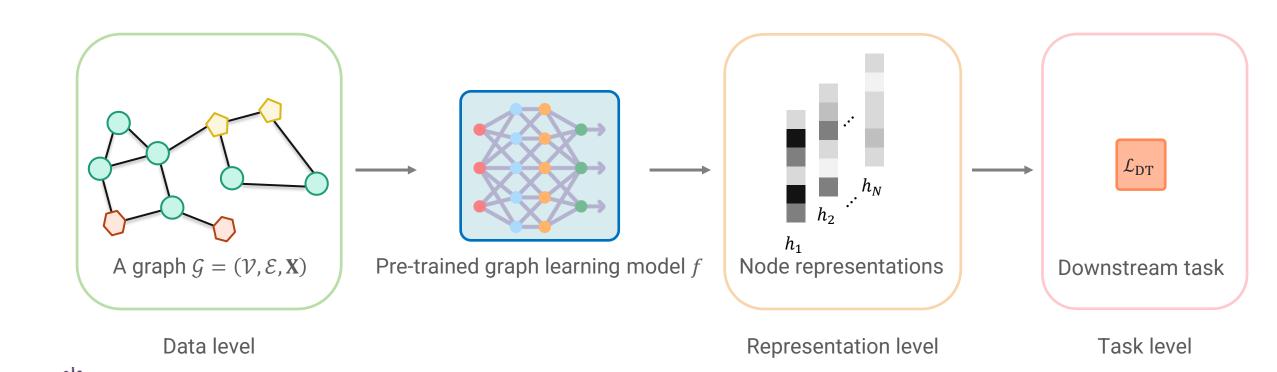
- Downstream tasks: node-level/graph-level/...
- Should be universal for different downstream tasks





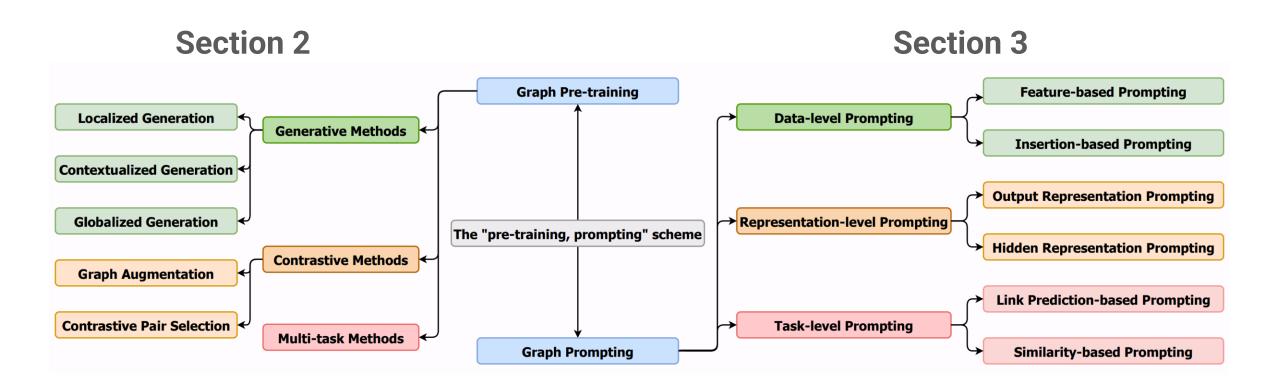
The "pre-training, prompting" scheme for graph learning models

Where Can We Design Prompts for Graph Prompting?



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Key Techniques in the "Pre-training, Prompting" Scheme





Section 2 Graph Pre-training for Graph Prompting

Zehong Wang

PhD Candidate

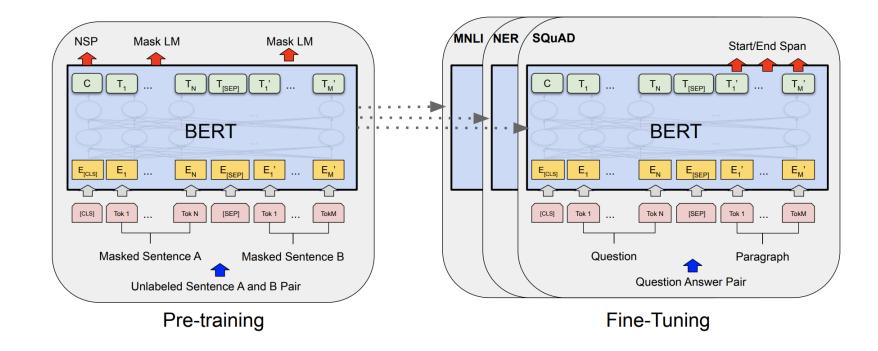
University of Notre Dame



From Supervised Learning to Self-supervised Learning

Generative Pre-training¹

- Generate the masked parts
- Masked Token Prediction
- Next Sentence Prediction

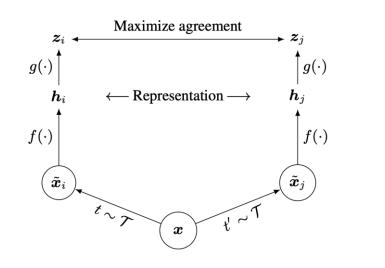




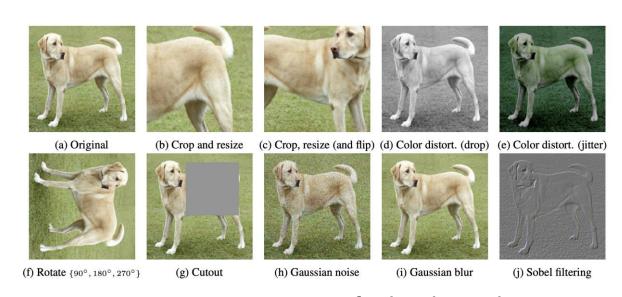
From Supervised Learning to Self-supervised Learning

Contrastive Pre-training¹

Pull positives together and push negatives apart for discriminative representations



Contrastive learning¹



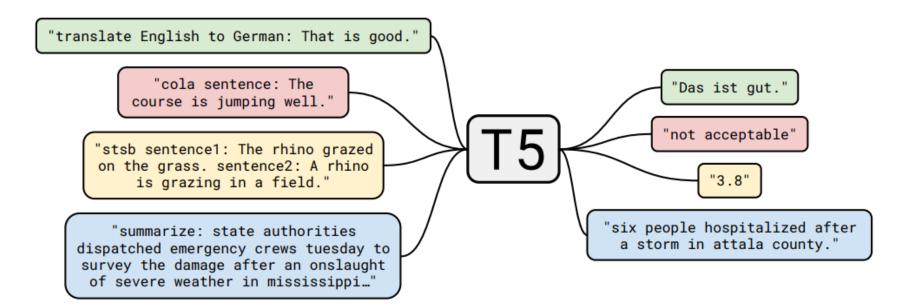
Data augmentation for harder tasks



From Supervised Learning to Self-supervised Learning

Multi-Task Pre-training¹

A single model to optimize multiple tasks, improving model capability and generalization



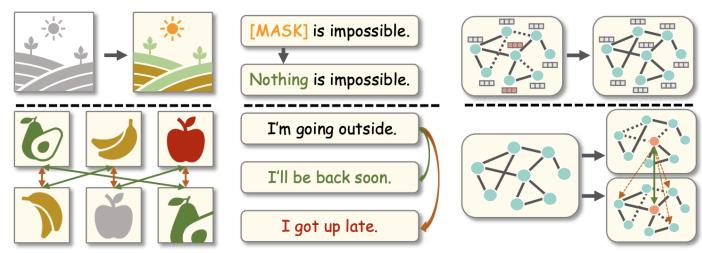


Pre-Training on Graphs

We need to carefully design pre-training tasks on graphs!

How to design pre-training tasks on graphs?

- Can we directly apply pre-training tasks on CV and NLP to graphs?
- Image/Text is in the Euclidean space
- Graph is in the non-Euclidean space



Toy examples of different pre-training tasks in CV, NLP, and graph learning¹

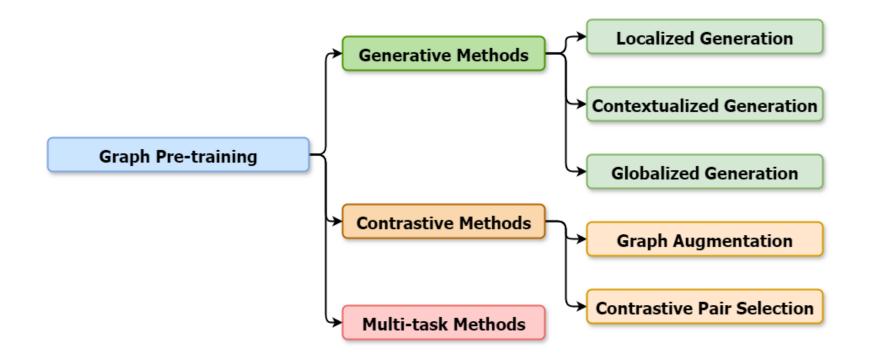
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[1] Liu, Yixin, et al. "Graph Self-Supervised Learning: A Survey." TKDE 2022.

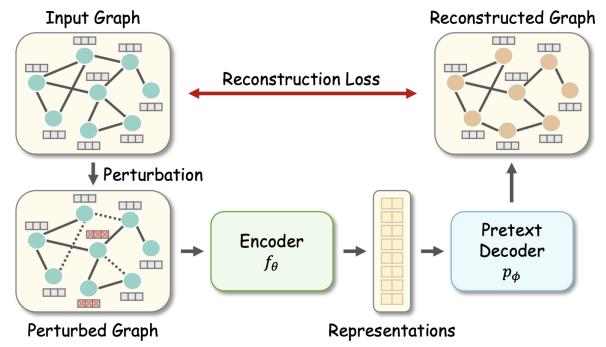
Taxonomy of Graph Pre-Training Techniques





Intuition: Corrupt the graph and reconstruct the corrupted parts

- Three types of generative methods
- Localized generation
- Contextualized generation
- Globalized generation

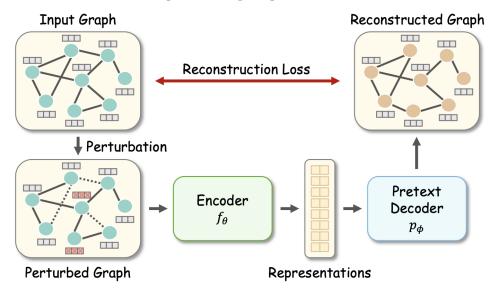


An illustration of generative methods for graph pre-training¹



[1] Liu, Yixin, et al. "Graph Self-Supervised Learning: A Survey." TKDE 2022.

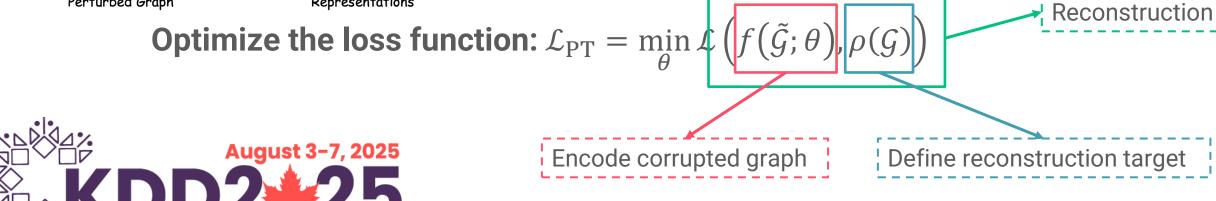
Intuition: Corrupt the graph and reconstruct the corrupted parts



G: the original graph

 $\tilde{\mathcal{G}}$: the corrupted graph

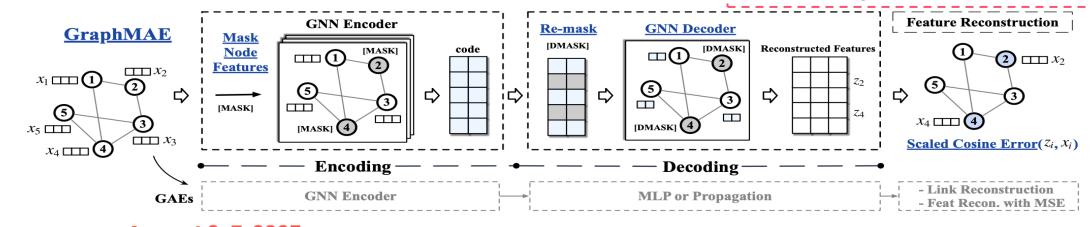
 θ : model parameters



Localized generation: reconstruct node features

- GraphMAE¹: Self-Supervised Masked Graph Autoencoders
- Corruption is to mask the node features $\tilde{\mathcal{G}} = mask_{node}(\mathcal{G})$
- Encoding $f(\tilde{\mathcal{G}}; \theta)$ is to encode the corrupted graphs **twice**
- Reconstruction is to reconstruct the masked node features

Could be extended to centrality level or clustering coefficient



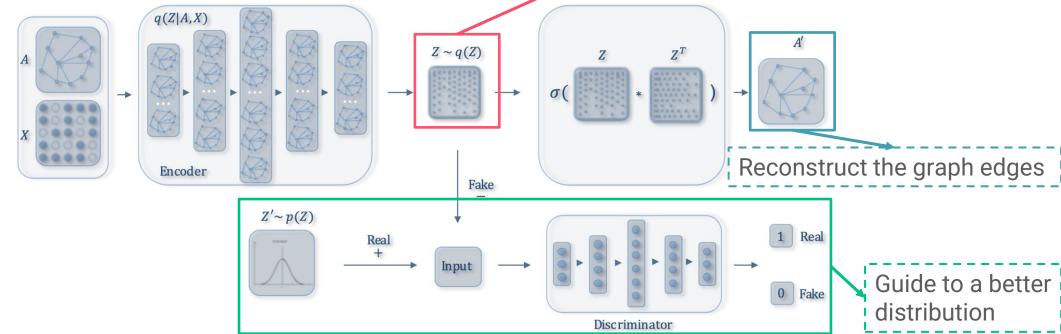
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2 2 2 5 [1

[1] Hou, Zhenyu, et al. "GraphMAE: Self-Supervised Masked Graph Autoencoders." KDD 2022.

Contextualized generation: reconstruct edges

Assume the corrupted embeddings are in this space

ARVGA¹: Adversarially Regularized Graph Autoencoder for Graph Embedding

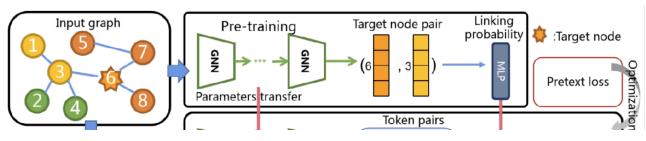




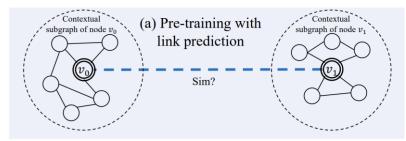
[1] Pan, Shirui, et al. "Adversarially Regularized Graph Autoencoder for Graph Embedding." IJCAI 2018.

Contextualized generation: reconstruct edges

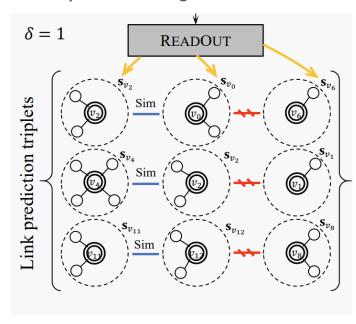
Many graph prompting methods adapt contextualized generation for pre-training



GPPT¹



GraphPrompt²



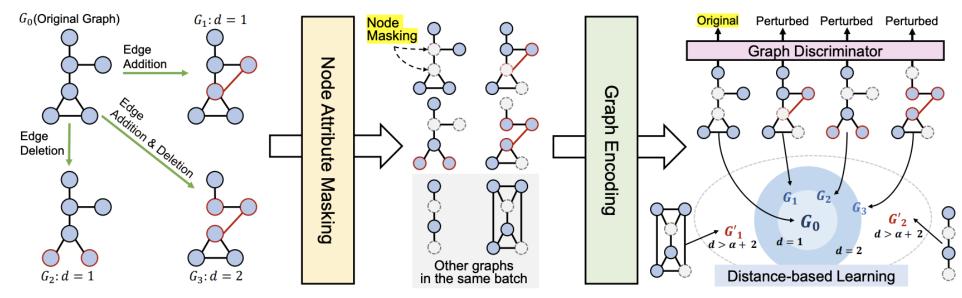
GraphPrompt+3



- [1] Sun, Mingchen, et al. "GPPT: Graph Pre-training and Prompt Tuning to Generalize Graph Neural Networks." KDD 2022.
- [2] Liu, Zemin, et al. "Graphprompt: Unifying pre-training and downstream tasks for graph neural networks." WWW 2023.
- [3] Yu, Xingtong, et al. "Generalized Graph Prompt: Toward a Unification of Pre-Training and Downstream Tasks on Graphs." TKDE 2024.

Globalized generation: reconstruct graph-level property

- Corruption: distance-based edge masking and random node feature masking
- Reconstruction: reconstruct the edit distance between graphs



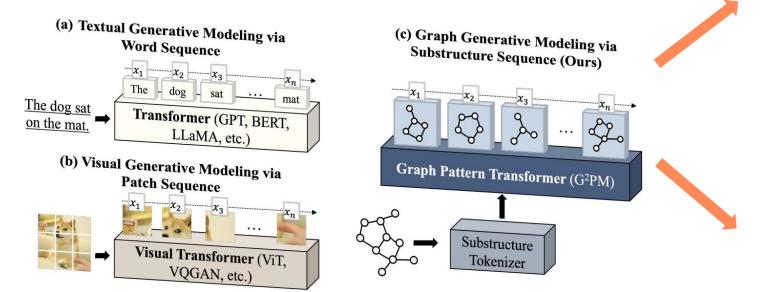


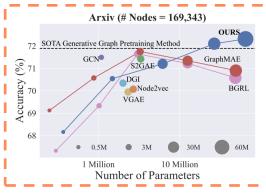
The workflow of D-SLA¹

[1] Kim, Dongki, Jinheon Baek, and Sung Ju Hwang. "Graph Self-supervised Learning with Accurate Discrepancy Learning." NeurIPS 2022.

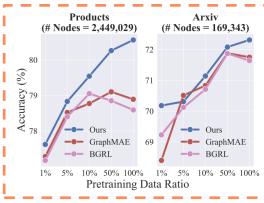
Others

- Scalable Graph Generative Modeling via Substructure Sequences (G2PM)
- Follow the general transformer pretraining on other domains, like CV and NLP





Model Scaling



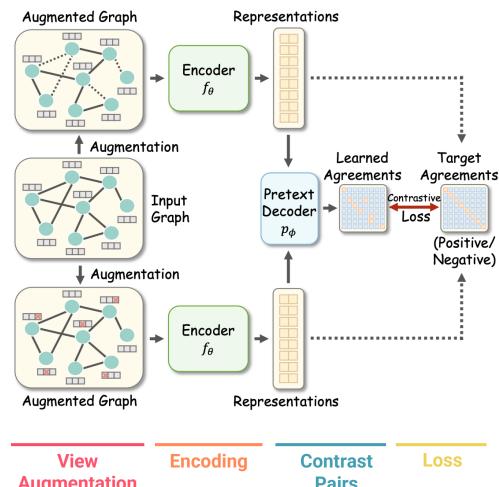
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[1] Wang, Zehong, et al. "Scalable Graph Generative Modeling via Substructure Sequences." arXiv preprint arXiv:2505.16130 (2025).

Contrastive Methods

Main steps

- 1. View augmentation
- Corrupt multiple graphs $\tilde{\mathcal{G}}_k = \operatorname{corrupt}_k(\mathcal{G})$.
- Encoding
- Encode each view $\mathbf{H}_{\mathbf{k}} = f(\tilde{\mathcal{G}}_{\mathbf{k}})$
- Contrast pairs
- Pick the contrastive pairs and levels
- Loss
- Maximize the similarity between positive pairs while minimizing the similarity between negative pairs



Augmentation

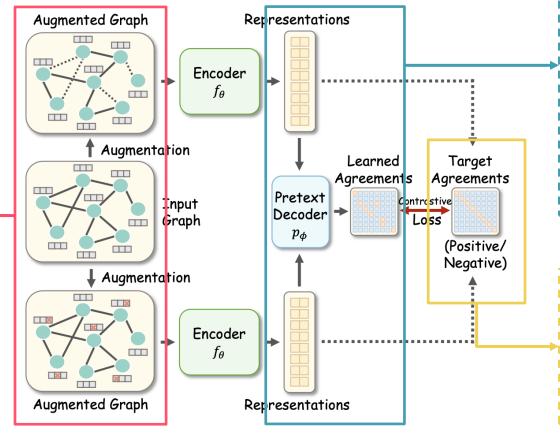
Pairs



Contrastive Methods

Augmentation:

- **1. Feature**, e.g., node feature masking, node feature shuffling, etc.
- **2. Structure**, e.g., edge perturbation, edge diffusion
- **3. Substructure**, e.g., egograph sampling, random walk sampling, etc.



Contrast Levels:

- 1. Local-Local, e.g., node-to-node contrast, node-to-subgraph contrast.
- **2. Local-Global**, e.g., node-to-graph contrast.
- **3. Global-Global**, e.g., graph-to-graph contrast.

Loss:

- 1. InfoNCE
- 2. JS divergence
- 3. ...

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View augmentation

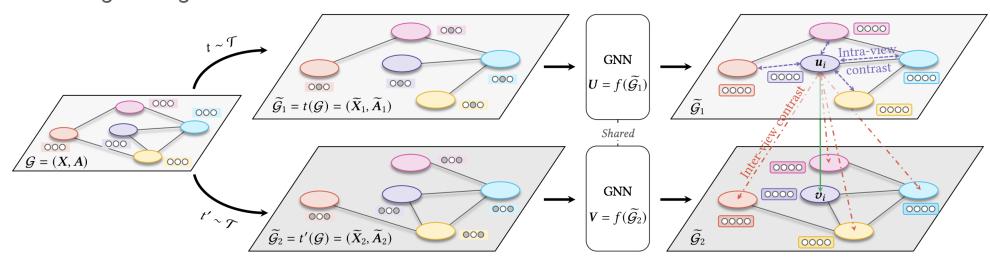
Encoding

Contrast Pairs

Loss

Local-to-local

 Augment two views of a single graph, treating the same node in these graphs as positives and the remaining as negatives



View Augmentation

Encoding

Contrast Pairs (InfoNCE)

The workflow of local-to-local contrastive methods¹



[1] Zhu, Yanqiao, et al. "Graph Contrastive Learning with Adaptive Augmentation." WWW 2021.

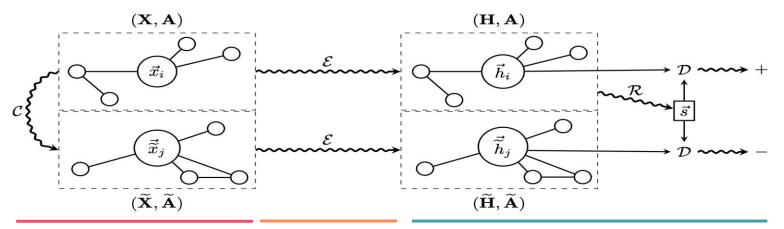
Local-to-local

- Augment two views of a single graph, treating the same node in these graphs as positives and the remaining as negatives
- GRACE¹: random node feature masking + random edge masking
- GCA²: centrality-based node feature masking + centrality-based edge masking

$$\ell(\boldsymbol{u}_i, \boldsymbol{v}_i) = \frac{e^{\theta(\boldsymbol{u}_i, \boldsymbol{v}_i)/\tau}}{\log \frac{e^{\theta(\boldsymbol{u}_i, \boldsymbol{v}_i)/\tau} + \sum_{k \neq i} e^{\theta(\boldsymbol{u}_i, \boldsymbol{v}_k)/\tau} + \sum_{k \neq i} e^{\theta(\boldsymbol{u}_i, \boldsymbol{u}_k)/\tau}}{\operatorname{positive pair}},$$
inter-view negative pairs intra-view negative pairs

Local-to-global

- Contrast pairs: node embedding vs graph embedding
- Deep Graph Infomax¹



View Augmentation

Encoding

Contrast Pairs

Augmentation:

node feature shuffling + edge perturbation

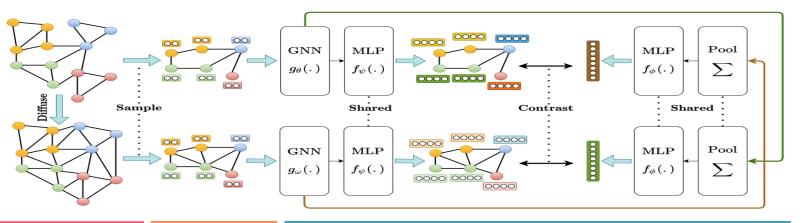
$$\mathsf{LOSS:} \ \, \mathcal{L} = \frac{1}{N+M} \left(\sum_{i=1}^{N} \mathbb{E}_{(\mathbf{X}, \mathbf{A})} \left[\log \mathcal{D} \left(\vec{h}_{i}, \vec{s} \right) \right] + \sum_{j=1}^{M} \mathbb{E}_{(\widetilde{\mathbf{X}}, \widetilde{\mathbf{A}})} \left[\log \left(1 - \mathcal{D} \left(\overrightarrow{\tilde{h}}_{j}, \vec{s} \right) \right) \right] \right)$$



[1] Veličković, Petar, et al. "Deep Graph Infomax." ICLR 2019.

Local-to-global

- Contrast pairs: node embedding vs graph embedding
- Multi-view contrastive learning¹



View Augmentation

Encoding

Contrast Pairs

Augmentation:

Graph diffusion + subgraph sampling

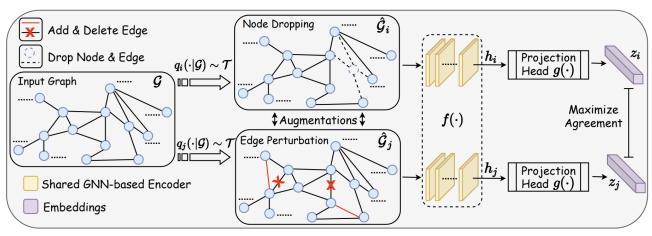
$$\text{Loss:} \quad \max_{\theta,\omega,\phi,\psi} \frac{1}{|\mathcal{G}|} \sum_{g \in \mathcal{G}} \left[\frac{1}{|g|} \sum_{i=1}^{|g|} \left[\text{MI} \left(\vec{h}_i^{\alpha}, \vec{h}_g^{\beta} \right) + \text{MI} \left(\vec{h}_i^{\beta}, \vec{h}_g^{\alpha} \right) \right] \right]$$



[1] Hassani, Kaveh, and Amir Hosein Khasahmadi. "Contrastive Multi-View Representation Learning on Graphs." ICML 2020...

Global-to-global

- Contrast pairs: graph embedding vs graph embedding
- GraphCL¹



View Augmentation

Encoding Contrast Pairs

Augmentation:

Random node dropping + edge perturbation

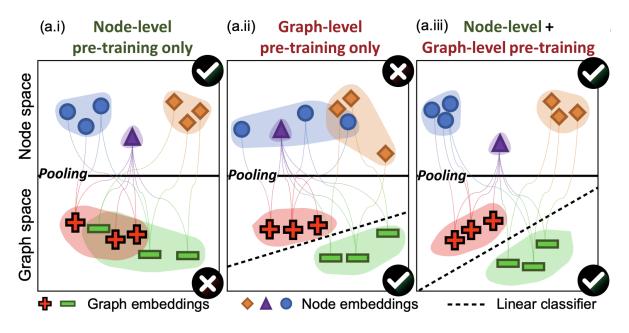
Loss:
$$\ell_n = -\log \frac{\exp(\sin(\boldsymbol{z}_{n,i}, \boldsymbol{z}_{n,j})/\tau)}{\sum_{n'=1, n' \neq n}^{N} \exp(\sin(\boldsymbol{z}_{n,i}, \boldsymbol{z}_{n',j})/\tau)}$$



[1] You, Yuning, et al. "Graph Contrastive Learning with Augmentations." NeurIPS 2020.

Jointly optimize multiple pre-training tasks

Intuition: inject diverse capability into a single model







[1] Hu, Weihua., et al. "Strategies For Pre-training Graph Neural Networks." ICLR 2020.

Jointly optimize multiple pre-training tasks

- Intuition: inject diverse capability into a single model
- Node-level & graph-level
- Attribute prediction & structure prediction

	Node-level	Graph-level
Attribute prediction	Attribute Masking	Supervised Attribute Prediction
Structure prediction	Context Prediction	Structural Similarity Prediction

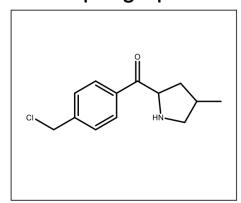
Different pre-training tasks¹



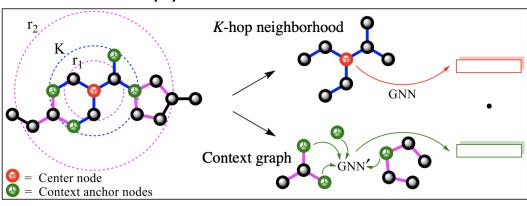
Jointly optimize multiple pre-training tasks

Intuition: inject diverse capability into a single model

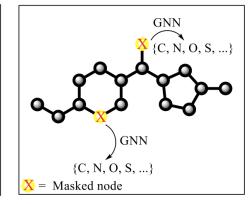
Input graph



(a) Context Prediction



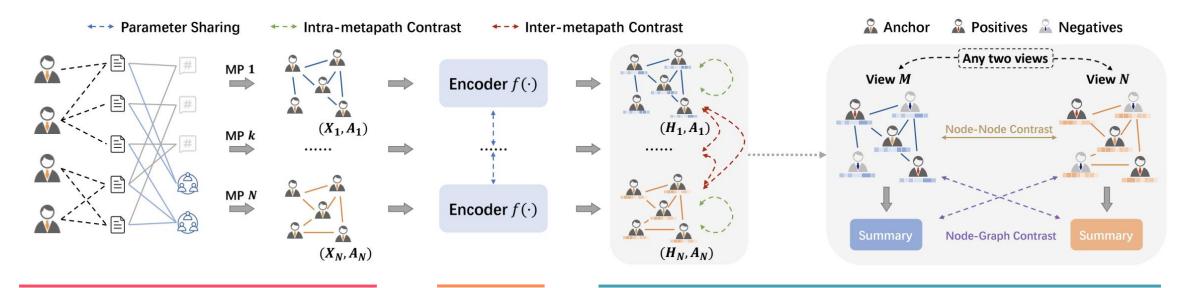
(b) Attribute Masking





Jointly optimize multiple pre-training tasks

- Heterogeneous graphs: Multi-view contrastive learning¹
- Use meta-paths on heterogeneous graphs to generate multiple views



Encoding

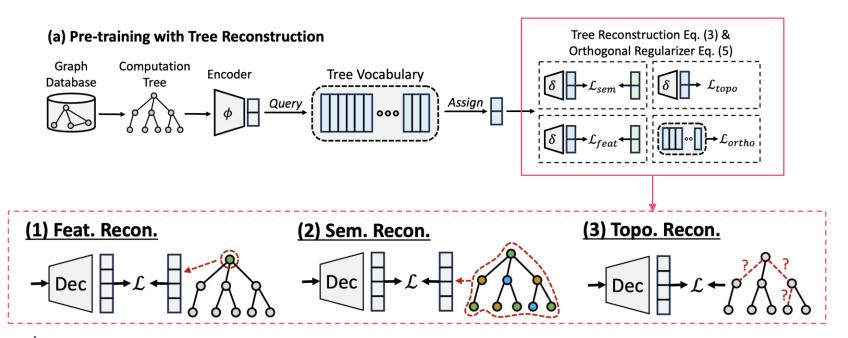


Contrast Pairs (local-to-local &local-to-global)

[1] Wang, Zehong, et al. "Heterogeneous Graph Contrastive Multi-view Learning." SDM 2023.

Jointly optimize multiple pre-training tasks

GFT: Graph Foundation Model with Transferable Tree Vocabulary¹



	Node	Link	Graph	Avg.				
Different Pre-training Tasks								
n/a	72.52	47.30	73.83	66.54				
w. \mathcal{L}_{sem}	76.25	90.39	<u>74.99</u>	<u>79.47</u>				
w. \mathcal{L}_{feat}	75.85	90.42	74.42	79.13				
w. \mathcal{L}_{topo}	75.50	90.28	74.57	78.96				
GFT	76.78	90.82	75.29	79.92				

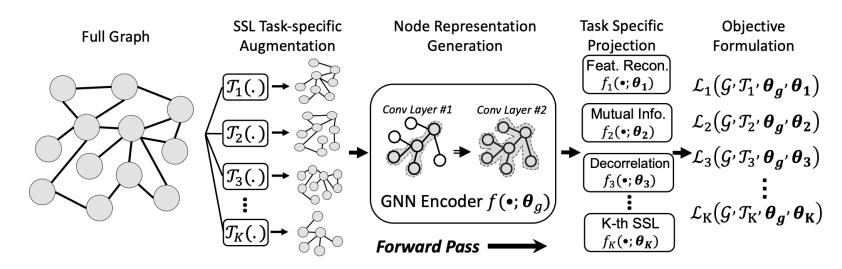
Jointly optimizing three-level tasks facilitates performance



[1] Wang, Zehong, et al. "GFT: graph foundation model with transferable tree vocabulary." NeurIPS 2024.

Jointly optimize multiple pre-training tasks

Multi-task Self-supervised Graph Neural Networks Enable Stronger Task Generalization¹

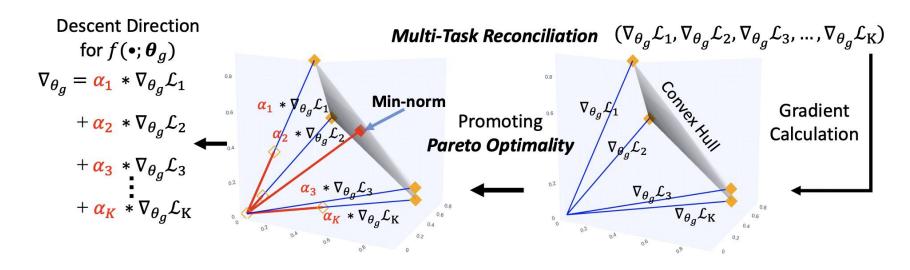


Multi-task learning on graphs



Jointly optimize multiple pre-training tasks

Multi-task Self-supervised Graph Neural Networks Enable Stronger Task Generalization¹



Multi-task reconciliation via Parato optimization



Jointly optimize multiple pre-training tasks

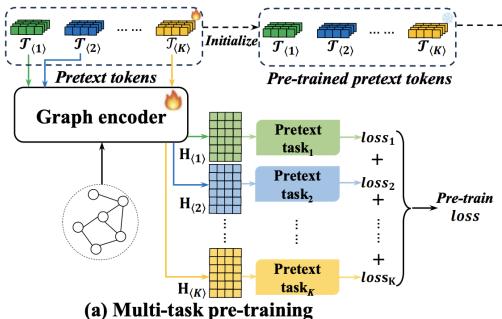
Multi-task Self-supervised Graph Neural Networks Enable Stronger Task Generalization¹

Method	Wiki.CS	PUBMED	Ам.Рното	Ам.Сомр.	Co.CS	Со.Рну.	Снам.	SQUIRREL	ACTOR	RANK
				Average P	ERFORMAN	CE				
FeatRec	74.06	69.48	84.76	77.76	86.61	75.20	64.66	52.43	31.63	4.6
TopoRec	70.44	66.32	85.18	79.41	85.23	77.45	61.20	52.89	38.56	5.0
RepDecor	69.54	67.42	83.74	78.49	84.49	78.31	58.98	52.19	36.28	5.8
MI-NG	71.89	67.35	85.33	79.95	83.01	75.00	63.72	49.56	30.60	5.7
MI-NSG	75.59	69.25	82.99	80.85	86.02	80.30	64.69	53.89	38.22	3.6
PARETOGNN	76.03	72.48	86.58	82.57	87.80	83.35	65.21	55.31	40.76	1.0
w/o Pareto	74.64	<u>69.82</u>	<u>85.82</u>	<u>82.09</u>	86.54	82.32	64.37	<u>54.90</u>	<u>40.12</u>	2.4



Jointly optimize multiple pre-training tasks

MultiGPrompt¹: multi-task pre-training for better task adaptation in prompting





Section 3 Techniques in Graph Prompting

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PhD Candidate

University of Virginia



Problem Formulation of Graph Prompting

Pre-training compatibility

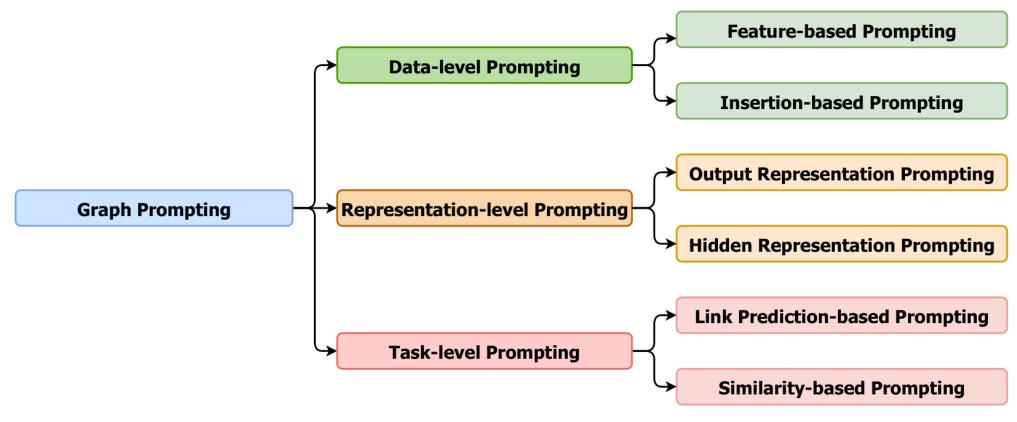
A graph learning model f is trained through a pre-training task \mathcal{L}_{PT} via self-supervised learning. During the prompting stage, graph prompting trains learnable prompts \mathcal{P} to adapt the pre-trained graph learning model f to a specific downstream task \mathcal{L}_{DT} .

Freeze pre-trained graph learning models

Downstream task universality



Taxonomy of Graph Prompting Techniques





Learn trainable prompts at the data level

- Intuition: modify the input graph data to fit specific downstream tasks
- Formulation

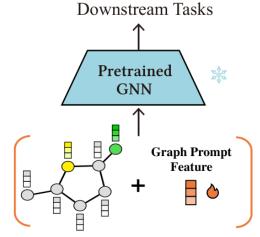
Given the input graph $\mathcal{G}=(\mathbf{A},\mathbf{X})$, data-level prompting \mathcal{T}^D transforms it into a prompted graph $\tilde{\mathcal{G}}=\left(\widetilde{\mathbf{A}},\widetilde{\mathbf{X}}\right)=\mathcal{T}^D\big((\mathbf{A},\mathbf{X}),\mathcal{P}\big) \text{ with learnable prompts } \mathcal{P} \text{ for adaptation.}$

- Two categories
- · Feature-based prompting
- Insertion-based prompting

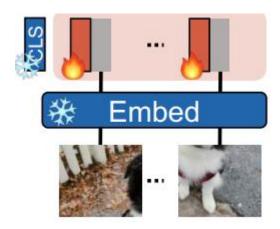


Feature-based prompting

- Intuition: solely modify the feature matrix by learning prompt features
- Inspired by prompting techniques in NLP and CV
- The graph topology remains unchanged $\rightarrow \tilde{\mathcal{G}} = (\mathbf{A}, \widetilde{\mathbf{X}}) = \mathcal{T}^D((\mathbf{A}, \mathbf{X}), \mathcal{P})$



Graph prompt feature (GPF)¹



Visual prompt tuning (VPT)²



[1] Fang, Taoran, et al. "Universal Prompt Tuning for Graph Neural Networks." NeurIPS. 2023.

[2] Jia, Menglin, et al. "Visual Prompt Tuning." ECCV 2022.

Feature-based prompting

- Goal: learn \mathbf{p}_i for $\tilde{\mathbf{x}}_i = \mathbf{x}_i + \mathbf{p}_i$
- Shared prompt features v.s. customized prompt features

Shared prompt features	Customized prompt features		
Fewer parameters	Increasing parameters in large-scale graphs		
Easy to train	Prone to overfitting		
Limited capability	More powerful		



Feature-based prompting

Customized prompt features with basis vectors¹

$$\tilde{\mathbf{x}}_i = \mathbf{x}_i + \mathbf{p}_i = \mathbf{x}_i + \sum_{m=1}^{M} \alpha_{i,m} \cdot \mathbf{b}_m$$

• GPF-plus¹: $\alpha_{i,m}$ as the softmax values of projected node feature \mathbf{x}_i

$$\alpha_{i,m} = \frac{\exp(a_m^{\mathrm{T}} \mathbf{x}_i)}{\sum_{k=1}^{M} \exp(a_k^{\mathrm{T}} \mathbf{x}_i)}$$

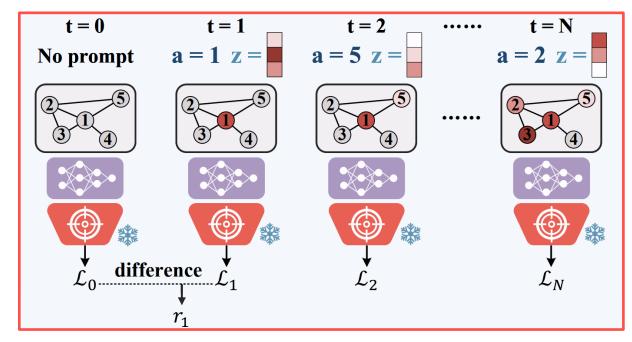
• SUPT 2 : α as the resulting scores derived from simple GNNs

$$\alpha = \widehat{\mathbf{A}}^m \left(\mathbf{X} \oplus \sum_{m=1}^M \mathbf{b}_m \right) \mathbf{W}$$

$$\widehat{\mathbf{A}} = (\mathbf{D} + \mathbf{I})^{-\frac{1}{2}} (\mathbf{A} + \mathbf{I}) (\mathbf{D} + \mathbf{I})^{-\frac{1}{2}}$$

Feature-based prompting

- Customized prompt features by reinforcement learning with hybrid action space¹
- Hybrid actions: discrete node index to prompt and its corresponding continuous prompt features
- States: node representations
- Reward function: instant loss decrease
- Policy network architecture: H-PPO with two parallel actor networks and a single critic network





Feature-based prompting

- Performance evaluation¹
- GPF+: prompts based on features may not obtain sufficient information
- SUPT: prompts based on both features and structures can improve performance
- RELIEF: selective methods are better than learning on all the nodes

	Tuning Strategy	BBBP	Tox21	ToxCast	SIDER
	FT	65.26 ± 1.05	71.54 ± 0.73	57.98 ± 0.42	53.45 ±0.49
XX	GPF	66.30 ± 0.94	71.26 ± 0.30	58.33 ± 0.27	53.65 ± 0.34
Щ	GPF-plus	66.12 ± 1.27	71.54 ± 0.63	58.43 ± 0.27	53.76 ± 1.15
Infomax	$SUPT_{soft}$	66.45 ± 0.85	71.82 ± 0.16	58.71 ± 0.44	53.72 ± 0.45
П	$SUPT_{hard}$	66.14 ± 0.85	71.55 ± 0.37	58.65 ± 0.33	53.82 ± 0.49
	RELIEF	67.93 ± 0.73	71.58 ± 0.13	58.78 ± 0.17	53.95 ± 0.40
ණ	FT	66.48 ± 0.44	72.32 ± 0.19	57.35 ±0.42	54.62 ±0.58
çi	GPF	66.67 ± 0.60	72.31 ± 0.30	58.01 ± 0.27	55.65 ± 1.92
AttrMasking	GPF-plus	66.29 ± 0.36	72.75 ± 0.38	57.91 ± 0.38	55.05 ±1.20
Š	$SUPT_{soft}$	66.28 ± 0.81	72.76 ± 0.41	58.28 ± 0.34	54.70 ± 1.03
Ħ	SUPThard	66.93 ± 0.91	72.75 ± 0.41	58.18 ± 0.44	55.20 ± 1.26
A	RELIEF	67.18 ± 0.55	72.40 ± 0.32	58.41 ± 0.14	56.54 ± 0.73
p	FT	62.82 ± 0.83	70.11 ±0.38	57.68 ±0.69	56.68 ± 0.78
re	GPF	61.65 ± 0.76	70.42 ± 0.29	58.51 ± 0.38	56.55 ± 0.46
xtI	GPF-plus	61.25 ± 0.73	70.12 ± 0.42	57.64 ± 0.70	56.86 ± 0.52
ıte	$SUPT_{soft}$	61.85 ± 1.56	70.37 ± 0.14	57.82 ± 0.37	56.57 ± 0.50
ContextPred	SUPThard	62.29 ± 1.41	70.40 ± 0.15	58.06 ± 0.39	56.34 ± 0.72
0	RELIEF	62.99 ± 0.67	70.51 ± 0.14	58.58 ± 0.04	56.89 ± 0.2
	FT	62.13 ±1.66	61.35 ±0.88	53.96 ±0.80	52.63 ± 0.71
	GPF	61.58 ± 1.81	59.92 ± 1.29	54.44 ± 0.31	51.21 ± 0.56
CCL	GPF-plus	62.19 ± 1.45	60.13 ± 0.52	54.43 ± 0.43	50.90 ± 0.78
	$SUPT_{soft}$	63.96 ± 0.85	60.13 ± 0.52	54.57 ± 0.76	51.44 ± 1.24
	$SUPT_{hard}$	64.15 ± 0.96	60.56 ± 0.20	54.72 ± 0.71	51.60 ± 0.85
	All in One	62.90 ± 3.77	61.49 ±0.96	54.72 ± 1.03	52.73 ± 0.84
	RELIEF	64.80 ± 0.69	61.45 ± 0.35	55.03 ±0.39	52.82 ± 0.59



Feature-based prompting

- Quantifying Prompts Impact¹
- Prompt Coverage Ratio (PCR): the proportion of nodes prompted at least once during prompting
- Average Prompt Magnitude (APM): the absolute values of all entries in prompts

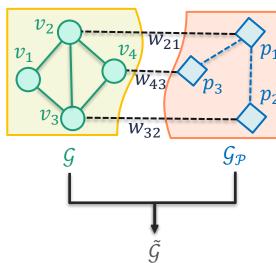
Tuning Strategy	PCR	APM (10^{-2})	OV. (10^{-2})	ROC-AUC
GPF	1.00	7.15	7.15	62.08
GPF-plus	1.00	6.69	6.69	62.38
$\mathrm{SUP}ar{\mathrm{T}}_{\mathrm{soft}}$	1.00	6.46	6.46	62.39
$\mathrm{SUPT}_{\mathrm{hard}}$	0.65	6.10	3.97	62.68
RELIEF	0.61	6.03	3.68	63.72

No need for graph prompting on every node!



Insertion-based prompting

- Intuition: insert additional prompt nodes as learnable prompts into the original graph
- $ilde{\mathcal{G}}$ includes the prompt nodes and the original graph nodes
- $\mathcal{P} = \{p_1, p_2, \cdots, p_M\}$: M learnable prompts as the feature vectors of the prompt nodes
- Key challenges
- The connection among the prompt nodes
- The connection among the prompt nodes and the original graph nodes





The connection among the prompt nodes

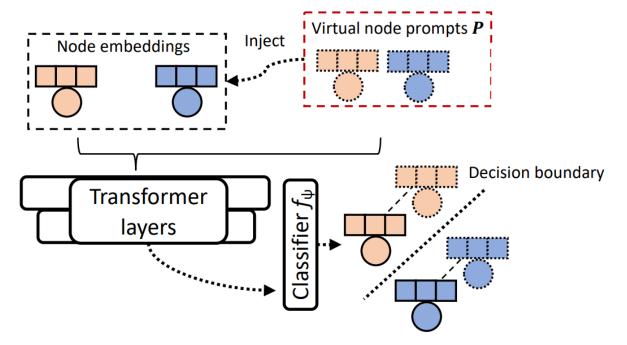
- Solution 1: free learnable parameters a_{ij} indicating how possible p_i and p_j should be connected¹
- Solution 2: the dot product of each prompt node pair
- Connect p_i and p_j if $\sigma(\mathbf{p}_i \cdot \mathbf{p}_j^{\mathrm{T}}) > \delta^1$
- Solution 3: treat the prompt nodes as independent^{1,2}

The connection among the prompt nodes and the original graph nodes

- Solution 1: the dot product between a prompt node and an original graph node
- $w_{ij} = \sigma(\mathbf{x}_i \cdot \mathbf{p}_j^{\mathrm{T}}) > \delta \text{ if } \sigma(\mathbf{x}_i \cdot \mathbf{p}_j^{\mathrm{T}}) > \delta^{1}$
- Solution 2: $\tilde{\mathbf{x}}_i = \mathbf{x}_i + \sum_{m=1}^{M} \mathbf{p}_m^{-1}$
- Solution 3: $N \times M$ free learnable parameters²

Insertion-based prompting for Graph Transformers ———— No worries about edge connections!

VNT¹: directly inject prompt nodes in the input of Graph Transformers





Learn trainable prompts at the representation level

- Intuition: apply learnable prompts to node representations
- Formulation

Given the (hidden) representation matrix $\mathbf{H}^{(l)}$ at the l-th layer, representation-level prompting \mathcal{T}^R transforms it into a prompted representation matrix $\widetilde{\mathbf{H}}^{(l)} = \mathcal{T}^R (\mathbf{H}^{(l)}, \mathcal{P})$ with learnable prompts \mathcal{P} for adaptation.

- Two categories
- Output representation prompting
- Hidden representation prompting



Output representation prompting

- Intuition: directly modify the output representations after the final layer
- Only the output representations are modified: $\tilde{\mathbf{h}}^{(L)} = \mathcal{T}^R(\mathbf{h}^{(L)}, \mathcal{P})$
- Straightforward design: GraphPrompt¹
- Element-wise multiplication: $\tilde{\mathbf{h}}_v^{(L)} = \mathbf{p}_v \odot \mathbf{h}_v^{(L)}$
- \mathbf{p}_{v} is shared by all the nodes
- Limitation: shared \mathbf{p}_{v} is insufficient



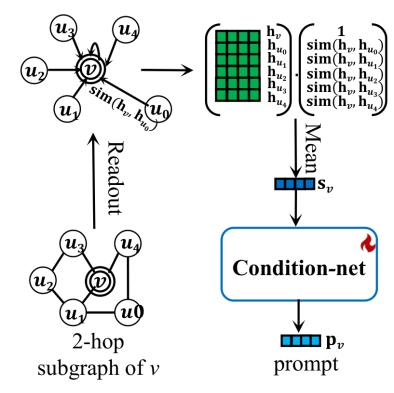
Output representation prompting

 Non-homophilic patterns of a node can be characterized by considering a multi-hop neighborhood around the node¹

$$\mathbf{s}_{v} = \frac{1}{\mathcal{N}_{2}(v)} \sum_{u_{j} \in \mathcal{N}_{2}(v)} \mathbf{h}_{v}^{(L)} \cdot \operatorname{sim}\left(\mathbf{h}_{v}^{(L)}, \mathbf{h}_{j}^{(L)}\right)$$

Obtain customized p_v through a condition-net²

$$\mathbf{p}_v = \varphi(\mathbf{s}_v) = \text{CondNet}(\mathbf{s}_v)$$



ProNoG¹



Output representation prompting

ProNoG¹ performs well on non-homophilic graphs

Methods	Wisconsin	Squirrel	Chameleon	Cornell	
GCN	21.39 ± 6.56	20.00 ± 0.29	25.11 ± 4.19	21.81 ± 4.71	
GAT	28.01 ± 5.40	21.55 ± 2.30	24.82 ± 4.35	23.03 ± 13.19	
H2GCN	23.60 ± 4.64	21.90 ± 2.15	25.89 ± 4.96	32.77 ± 14.88	
FAGCN	35.03 ± 17.92	20.91 ± 1.79	22.71 ± 3.74	28.67 ± 17.64	
DGI	28.04 ± 6.47	20.00 ± 1.86	19.33 ± 4.57	32.54 ± 15.66	
GRAPHCL	29.85 ± 8.46	21.42 ± 2.22	27.16 ± 4.31	24.69 ± 14.06	
DSSL	28.46 ± 10.31	20.94 ± 1.88	27.92 ± 3.93	20.36 ± 5.38	
GRAPHACL	34.57 ± 10.46	24.44 ± 3.94	26.72 ± 4.67	33.17 ± 16.06	
GPPT	27.39 ± 6.67	20.09 ± 0.91	24.53 ± 2.55	25.09 ± 2.92	
GRAPHPROMPT	31.48 ± 5.18	21.22 ± 1.80	25.36 ± 3.99	31.00 ± 13.88	
GraphPrompt+	31.54 ± 4.54	21.24 ± 1.82	25.73 ± 4.50	31.65 ± 14.48	
ProNoG	44.72 ± 11.93	24.59 ± 3.41	30.67 ± 3.73	37.90 ± 9.31	



Hidden representation prompting

- Intuition: modify node representations with layer-wise prompts
- More parameters provide more flexibility
- GraphPrompt+1: an advanced version of GraphPrompt
- Learnable prompts at each layer $\mathcal{P} = \{\mathbf{p}^{(0)}, \mathbf{p}^{(1)}, \mathbf{p}^{(2)}, \cdots, \mathbf{p}^{(L)}\}$
- Prompted representation fusion with learnable coefficients

$$\widetilde{\mathbf{H}} = \sum_{l=0}^{L} w^{(l)} \cdot \widetilde{\mathbf{H}}^{(l)}$$

Hidden representation prompting

- EdgePrompt+1: learn edge prompts for each edge
- $e_{ij}^{(l)}$: prompt vector on edge (v_i, v_j) at the l-th layer
- Without edge prompts

$$\mathbf{h}_i^{(l)} = \mathsf{COMB}^{(l)}\left(\mathbf{h}_i^{(l-1)}, \mathsf{AGG}^{(l)}\left(\left\{\mathbf{h}_j^{(l-1)} \colon v_j \in \mathcal{N}(v_i)\right\}\right)\right)$$

With edge prompts

$$\mathbf{h}_i^{(l)} = \mathsf{COMB}^{(l)}\left(\mathbf{h}_i^{(l-1)}, \mathsf{AGG}^{(l)}\left(\left\{\boldsymbol{h}_j^{(l-1)} \colon v_j \in \mathcal{N}(v_i)\right\}, \left\{\mathbf{e}_{ij}^{(l)} \colon v_j \in \mathcal{N}(v_i)\right\}\right)\right)$$



Hidden representation prompting

- EdgePrompt+1: learn edge prompts for each edge
- Compute edge prompts as the weighted average of the anchor prompts

$$\mathbf{e}_{ij}^{(l)} = \sum_{m=1}^{M} b_{ijm}^{(l)} \mathbf{p}_{m}^{(l)}$$

• $\mathbf{b}_{ij}^{(l)}$ is computed using a score function $\varphi^{(l)}$

$$\mathcal{P}^{(l)} = \left\{ \mathbf{p}_1^{(l)}, \mathbf{p}_2^{(l)}, \cdots, \mathbf{p}_M^{(l)} \right\}$$

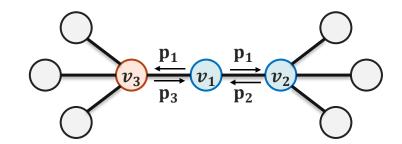
$$\mathbf{b}_{ij}^{(l)} = \operatorname{Softmax}\left(\varphi^{(l)}(v_i, v_j)\right)$$

$$\varphi^{(l)}(v_i, v_j) = \text{LeakyReLU}\left(\left[\mathbf{h}_i^{(l-1)} || \mathbf{h}_j^{(l-1)}\right] \cdot \mathbf{W}^{(l)}\right)$$

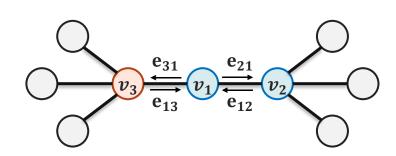


Hidden representation prompting

- Why EdgePrompt+ works?
- Prompting on nodes: add learnable prompts to node features or representations¹
- Limitation: \mathbf{p}_i will be uniformly aggregated by neighboring nodes



- Prompting on edges: add learnable prompts on edges²
- \mathbf{e}_{ij} provides customized prompts to different neighboring nodes
- Each node broadcasts distinct prompts to its neighbors





Hidden representation prompting

- EdgePrompt+ is more powerful than EdgePrompt
- → Customized edge prompts > shared edge prompts
- EdgePrompt+ is compatible with both generative and contrastive pre-training strategies
- GPF-plus is competitive among data-level prompting methods

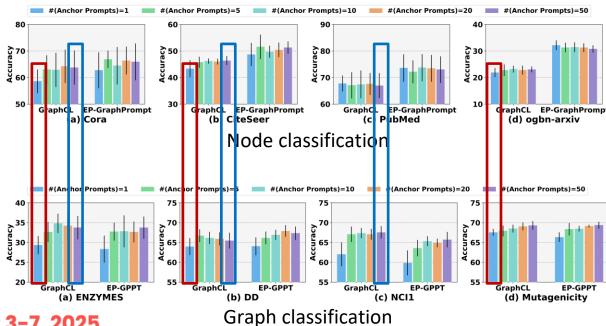
Pre-training Strategies	Tuning Methods	ENZYMES	DD	NCI1	NCI109	Mutagenicity
GraphCL	Classifier Only GraphPrompt ALL-in-one GPF GPF-plus EdgePrompt EdgePrompt+	$\begin{array}{c} 30.50 \pm 1.16 \\ 27.83 \pm 1.61 \\ 25.92 \pm 0.55 \\ 30.08 \pm 1.25 \\ \hline 31.00 \pm 1.50 \\ 29.50 \pm 1.57 \\ \hline \textbf{34.00} \pm 1.25 \\ \end{array}$	$\begin{array}{c} 62.89 \pm 2.19 \\ 64.33 \pm 1.79 \\ 66.54 \pm 1.82 \\ 64.54 \pm 2.22 \\ 67.26 \pm 2.29 \\ 64.16 \pm 2.13 \\ 67.98 \pm 2.05 \end{array}$	$62.49_{\pm 1.95} \\ 63.19_{\pm 1.71} \\ 57.52_{\pm 2.61} \\ 62.66_{\pm 1.83} \\ 64.56_{\pm 1.10} \\ 63.05_{\pm 2.11} \\ 66.30_{\pm 2.54}$	$\begin{array}{c} 61.68_{\pm 0.93} \\ 62.18_{\pm 0.48} \\ 62.74_{\pm 0.78} \\ 62.29_{\pm 0.90} \\ 62.84_{\pm 0.22} \\ 62.59_{\pm 0.93} \\ 66.52_{\pm 0.91} \end{array}$	$66.62_{\pm 1.87}$ $67.62_{\pm 0.65}$ $63.43_{\pm 2.53}$ $66.54_{\pm 1.85}$ $66.82_{\pm 1.63}$ $66.87_{\pm 1.88}$ $67.47_{\pm 2.37}$
SimGRACE	Classifier Only GraphPrompt ALL-in-one GPF GPF-plus EdgePrompt EdgePrompt+	$\begin{array}{c} 27.07_{\pm 1.04} \\ 26.87_{\pm 1.47} \\ 25.73_{\pm 1.18} \\ 28.53_{\pm 1.76} \\ 27.33_{\pm 2.01} \\ \hline 29.33_{\pm 2.30} \\ \hline 32.67_{\pm 2.53} \end{array}$	$\begin{array}{c} 61.77 \pm 2.40 \\ 62.58 \pm 1.84 \\ 65.16 \pm 1.47 \\ 65.64 \pm 0.70 \\ 67.20 \pm 1.56 \\ 63.97 \pm 2.14 \\ 67.72 \pm 1.62 \end{array}$	$\begin{array}{c} 61.27_{\pm 3.64} \\ 62.45_{\pm 1.52} \\ \overline{58.52_{\pm 1.59}} \\ 61.45_{\pm 3.13} \\ 61.61_{\pm 2.89} \\ 62.02_{\pm 3.02} \\ \mathbf{67.07_{\pm 1.96}} \end{array}$	$\begin{array}{c} 62.12{\pm}1.10 \\ 62.41{\pm}0.69 \\ 62.01{\pm}0.66 \\ 61.90{\pm}1.26 \\ 62.84{\pm}0.23 \\ 62.02{\pm}1.03 \\ \textbf{66.53}{\pm}1.30 \\ \end{array}$	$\begin{array}{c} 67.36 \pm 0.71 \\ 68.03 \pm 0.78 \\ \hline 64.43 \pm 1.00 \\ 67.19 \pm 0.74 \\ \hline 67.69 \pm 0.64 \\ 67.55 \pm 0.85 \\ \hline 68.31 \pm 1.36 \\ \end{array}$
EP-GPPT	Classifier Only GraphPrompt ALL-in-one GPF GPF-plus EdgePrompt EdgePrompt+	$\begin{array}{c} 29.08_{\pm 1.35} \\ 26.67_{\pm 1.60} \\ 24.92_{\pm 1.33} \\ 28.33_{\pm 1.73} \\ 29.25_{\pm 1.30} \\ 28.33_{\pm 3.41} \\ \textbf{32.75}_{\pm 2.26} \end{array}$	$\begin{array}{c} 62.12_{\pm 2.82} \\ 61.61_{\pm 1.91} \\ 63.61_{\pm 2.12} \\ 63.48_{\pm 2.08} \\ \textbf{66.92}_{\pm \textbf{2.34}} \\ 64.03_{\pm 2.26} \\ 66.16_{\pm 1.60} \end{array}$	$\begin{array}{c} 56.85_{\pm 4.35} \\ 58.77_{\pm 0.97} \\ 59.14_{\pm 2.12} \\ 58.14_{\pm 4.16} \\ 62.93_{\pm 3.23} \\ 59.85_{\pm 3.15} \\ \textbf{63.58}_{\pm 2.07} \end{array}$	$\begin{array}{c} 62.27_{\pm 0.78} \\ 62.16_{\pm 0.89} \\ 59.70_{\pm 1.37} \\ 62.52_{\pm 1.39} \\ 64.13_{\pm 1.42} \\ 62.98_{\pm 1.44} \\ \textbf{65.15}_{\pm 1.60} \end{array}$	$\begin{array}{c} 66.30_{\pm 1.78} \\ 66.37_{\pm 1.17} \\ 64.86_{\pm 1.60} \\ 66.10_{\pm 0.96} \\ 67.57_{\pm 1.45} \\ 66.36_{\pm 1.22} \\ 68.35_{\pm 1.57} \end{array}$
EP-GraphPrompt	Classifier Only GraphPrompt ALL-in-one GPF GPF-plus EdgePrompt EdgePrompt+	$\begin{array}{c} 31.33_{\pm 3.22} \\ 30.20_{\pm 1.93} \\ 29.07_{\pm 1.16} \\ 30.93_{\pm 1.76} \\ 30.67_{\pm 3.06} \\ 30.80_{\pm 2.09} \\ \textbf{33.27}_{\pm 2.71} \end{array}$	$62.58 \pm 2.40 \\ 64.72 \pm 1.98 \\ 65.60 \pm 2.38 \\ 66.21 \pm 1.66 \\ \textbf{67.50} + \textbf{2.45} \\ 65.87 \pm 1.35 \\ 67.47 \pm 2.14$	$\begin{array}{c} 62.09{\pm}2.31 \\ 62.57{\pm}1.45 \\ 58.67{\pm}2.42 \\ 61.80{\pm}2.78 \\ 62.59{\pm}2.09 \\ 61.75{\pm}2.49 \\ \textbf{65.06}{\pm}1.84 \end{array}$	$\begin{array}{c} 60.19_{\pm 1.71} \\ 62.32_{\pm 0.95} \\ 57.69_{\pm 1.08} \\ 62.27_{\pm 1.18} \\ \hline 61.98_{\pm 1.60} \\ \hline 62.33_{\pm 1.65} \\ \hline 64.64_{\pm 1.57} \end{array}$	$\begin{array}{c} 65.13 \pm 0.81 \\ \underline{65.85 \pm 0.65} \\ \overline{64.66 \pm 0.76} \\ \underline{65.61 \pm 0.59} \\ \underline{65.51 + 1.10} \\ \underline{65.77 \pm 0.90} \\ \mathbf{66.42 \pm 1.31} \end{array}$



Representation-level Prompting

Hidden representation prompting

- One anchor prompt is insufficient in most cases
- Two many anchor prompts may not improve performance (hard to train)





Particularly classification tasks

Learn trainable prompts at the task level

- Intuition: reformulate downstream tasks into alternative forms
- Formulation

Given a downstream task $\mathcal{L}_{\mathrm{DT}}$ (e.g., node classification), task-level prompting \mathcal{T}^T transforms it into a different task $\tilde{\mathcal{L}}_{\mathrm{DT}} = \mathcal{T}^T(\mathcal{L}_{\mathrm{DT}}, \mathcal{P})$ with learnable prompts \mathcal{P} for adaptation.

- Two categories
- Link prediction-based prompting
- Similarity-based prompting



Link prediction-based prompting

Recall: the gap between edge prediction for pre-training and node classification as the downstream task

Phase	Pre-training stage Downstream stage		
Illustration			
Task	Edge prediction	Node classification	
Involved embeddings	A pair of nodes A single node		
Prediction	Edge probabilities Node class probabilities		



Link prediction-based prompting

- Intuition: convert node classification to edge prediction
- Pre-training stage: edge prediction with positive and negative pairs

Positive pair



$$g(v_1, v_2) = 1$$

Negative pair

$$v_1$$
 v_2

$$g(v_1, v_2) = 0$$

Pre-training objective

$$\min_{\pi_{\text{GNN}}, \phi_{\text{Proj}}} \sum_{(v_i, v_j)} \mathcal{L}_{\text{CE}} \left(\phi_{\text{Proj}}(\mathbf{h}_i, \mathbf{h}_j), g(v_i, v_j) \right)$$



Link prediction-based prompting

- Intuition: convert node classification to edge prediction
- Downstream stage: construct positive and negative pairs using learnable task tokens

Positive pair



$$g(v_1, y_1) = 1$$

Negative pair

$$v_1$$
 v_2

$$g(v_1, y_2) = 0$$

Downstream objective

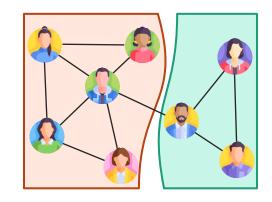
$$\min_{\pi_{\text{GNN}}, \phi_{\text{Proj}}, \mathbf{E}} \sum_{(v_i, \mathbf{y}_c)} \mathcal{L}_{\text{CE}} \left(\phi_{\text{Proj}}(\mathbf{h}_i, \mathbf{e}_c), g(v_i, \mathbf{y}_c) \right)$$



Link prediction-based prompting

- GPPT: one global task token E is insufficient for all nodes¹
- Task tokens should vary with clusters
- For each cluster m, train an independent task token \mathbf{E}^m

$$\min_{\pi_{\text{GNN}}, \phi_{\text{Proj}}, \mathbf{E^1}, \dots, \mathbf{E^M}} \sum_{(v_i, y_c)} \mathcal{L}_{\text{CE}} \left(\phi_{\text{Proj}}(\mathbf{h}_i, \mathbf{e}_c^m), g(v_i, y_c) \right)$$



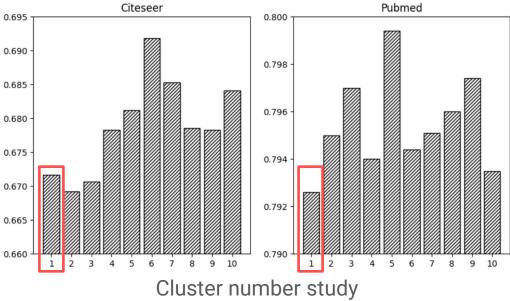
- Use structure tokens to replace node embeddings: $\mathbf{e}_i = a_i \cdot \mathbf{h}_i + \sum_{v_j \in \mathcal{N}(v_i)} a_j \cdot \mathbf{h}_j$
- Final objective

$$\min_{\pi_{\text{GNN}}, \phi_{\text{Proj}}, \mathbf{E^1}, \cdots, \mathbf{E^M}} \sum_{(v_i, y_c)} \mathcal{L}_{\text{CE}} \left(\phi_{\text{Proj}}(\mathbf{e_i}, \mathbf{e_c^m}), g(v_i, y_c) \right) + \lambda \sum_{m} \left\| \mathbf{E}^M (\mathbf{E}^M)^{\text{T}} - \mathbf{I} \right\|_F^2$$



Link prediction-based prompting

- The impact of cluster numbers in GPPT¹
- The performance of GPPT is significantly damaged with one cluster





Similarity-based prompting

Intuition: compare graph representations to class prototypes using contrastive loss

$$\min_{\mathcal{P}} \sum_{(x,y)\in\mathcal{D}} -\log \frac{\exp(\sin(\mathbf{h}_i, \mathbf{s}_y)/\tau)}{\sum_{c\in\mathcal{Y}} \exp(\sin(\mathbf{h}_i, \mathbf{s}_c)/\tau)}$$

- How to get class prototypes?
- GraphPrompt, GraphPrompt+, ProNoG: use the average of instance representations belonging to class c
- HetGPT¹: initialized using average representation and tuned while prompting

Comparison of Graph Prompting Techniques

Technique Categories	Prompting Stage	Prompting Strategies	Single Forward Pass	DT Universality
Data-level prompting	Graph data	Feature-based prompting	×	✓
		Insertion-based prompting	×	√
Representation-level prompting	Node representations	Output representation prompting	✓	/
		Hidden representation prompting	×	✓
Task-level prompting	Downstream tasks	Link prediction-based prompting	✓	Х
		Similarity-based prompting	√	X



Section 4 Summary and Future Directions

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Summary

Graph prompting

- Objective gap between pre-training and downstream tasks
- Example: link prediction → node classification
- Graph pre-training methods: the foundation step of graph prompting
- Generative methods, contrastive method, multi-task methods
- Mainstream techniques in graph prompting
- Data-level, representation-level, task-level techniques



Benchmarks and datasets

- Standard experimental settings for performance evaluation
- Cross-dataset & cross-domain evaluation
- One existing benchmark¹



🍀 ProG: A Unified Python Library for Graph Prompting 🍀

| Quick Start | Paper | Media Coverage | Call For Contribution |





Theoretical foundation

Empirical improvements → theoretical guarantees

Theorem 3. Given a GPF-like prompt vector p_{ω} , if a GCN model F_{θ} has non-linear function layers but the model's weight matrix is row full-rank, then there exists an optimal ω for any input graph G such that $P_{\omega}(G) \in B_G$.

Theorem 4. Given the All-in-One-like prompt graph SG_{ω} (a subgraph containing prompt tokens and token structures), if a GCN model F_{θ} does not have any non-linear transformations, or has non-linear layers but the model's weight matrix is row full-rank, then there exists an optimal ω for any input graph G such that $P_{\omega}(G) \in B_G$.

The upper bound of graph prompting¹



Theoretical foundation

Empirical improvements → theoretical guarantees

Theorem 1. (Universal Capability of GPF) Given a pre-trained GNN model f, an input graph $\mathcal{G}: (\mathbf{A}, \mathbf{X})$, an arbitrary prompting function $\psi_t(\cdot)$, for any prompted graph $\hat{\mathcal{G}}: (\hat{\mathbf{A}} \in \mathbb{A}, \hat{\mathbf{X}} \in \mathbb{X})$ in the candidate space of the graph template $\mathcal{G}^* = \psi_t(\mathcal{G})$, there exists a GPF extra feature vector \hat{p} that satisfies:

$$f(\mathbf{A}, \mathbf{X} + \hat{p}) = f(\hat{\mathbf{A}}, \hat{\mathbf{X}}) \tag{11}$$

Universal capability of graph prompting¹



Theoretical foundation

Empirical improvements → theoretical guarantees

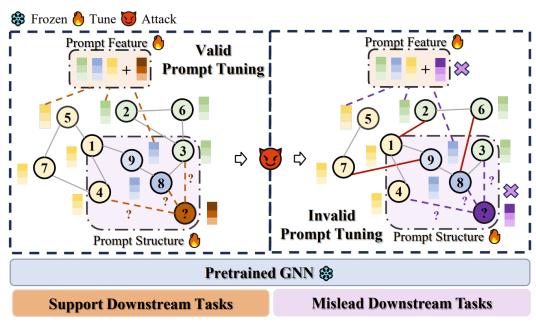
Theorem 1. Given a random graph $\mathcal{G} \sim CSBM(\boldsymbol{\mu}_1, \boldsymbol{\mu}_2, p, q)$ and a pre-trained GCN model f, there always exist a set of $M \geq 2$ anchor prompts $\mathcal{P} = \{\boldsymbol{p}_1, \boldsymbol{p}_2, \cdots, \boldsymbol{p}_M\}$ and the score vectors $\boldsymbol{b}_{i,j}$ for each edge (v_i, v_j) that improve the expected distance after GCN operation between classes c_1 and c_2 to T times without using edge prompts, where $T \in (1, 1 + \frac{p}{|p-q|}]$.

Separability improvements by graph prompting¹



Attacks & defense in graph prompting

A new attack and defense perspective by graph prompting



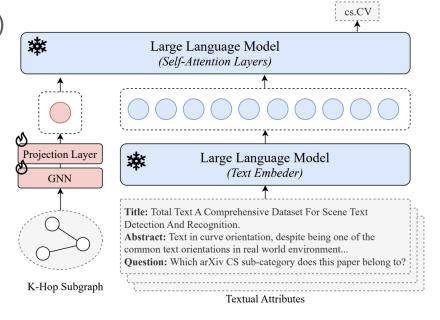
Adversarial attacks in graph prompting¹



[1] Song, Shuhan, et al. "GPromptShield: Elevating Resilience in Graph Prompt Tuning Against Adversarial Attacks." ICLR. 2025.

LLM Incorporation for graph prompting

- Graph prompting with semantic information in graph data
- Text-attributed graphs (TAGs)



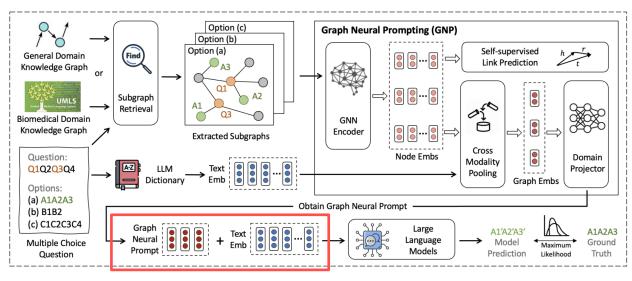




[1] Liu, Zheyuan, et al. "Can we Soft Prompt LLMs for Graph Learning Tasks?." WWW 2024.

LLM Incorporation for graph prompting

- Graph prompting with semantic information in graph data
- Knowledge graphs (KGs)

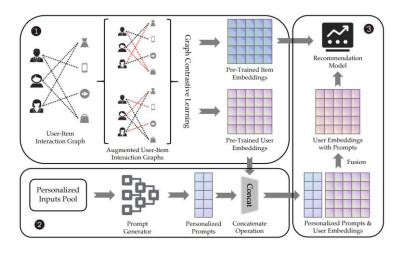




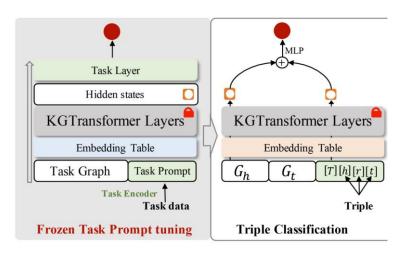
Graph Neural Prompting (GNP)¹

[1] Tian, Yijun, et al. "Graph Neural Prompting with Large Language Models." AAAI 2024.

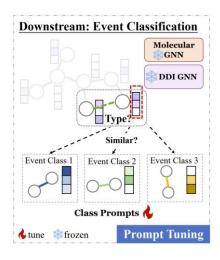
Applications in various domains



Recommendation systems¹



Knowledge engineering²



Biology and medicine³



[1] Yang, Haoran, et al. "An Empirical Study Towards Prompt-Tuning for Graph Contrastive Pre-Training in Recommendations." NeurIPS 2023.

[2] Zhang, Wen, et al. "Structure Pretraining and Prompt Tuning for Knowledge Graph Transfer." WWW 2023.

[3] Wang, Yingying, et al. "DDIPrompt: Drug-Drug Interaction Event Prediction based on Graph Prompt Learning." CIKM. 2024.

THANK YOU!

